Unsupervised Learning of Morphology with Graph Sampling

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Abstract

We introduce a language-independent, graph-based probabilistic model of morphology, which uses transformation rules operating on whole words instead of the traditional morphological segmentation. The morphological analysis of a set of words is expressed through a graph having words as vertices and structural relationships between words as edges. We define a probability distribution over such graphs and develop a sampler based on the Metropolis-Hastings algorithm. The sampling is applied in order to determine the strength of morphological relationships between words, filter out accidental similarities and reduce the set of rules necessary to explain the data. The model is evaluated on the task of finding pairs of morphologically similar words, as well as generating new words. The results are compared to a state-of-the-art segmentation-based approach.

1 Introduction

The aim of unsupervised learning of morphology is to explain structural similarities between words of a language and discover mechanisms allowing one to predict or analyze unseen words using only a plain wordlist or an unannotated corpus as input. A vast majority of approaches to this problem concentrates on morphological segmentation, i.e. segmentation of words into minimal structural units, called morphs (Hammarström and Borin, 2011), usually employing statistical or machine learning methods.

While the segmentation approach has proven successful in some applications (especially compound splitting), it is known to suffer from serious limitations, like e.g. its intrinsic difficulty of handling non-concatenative morphology. Furthermore, phenomena like morphophonological rules (reflected by the orthography), allomorphs, or interactions between morphemes, are especially difficult to discover in an unsupervised setting, which is why most approaches limit themselves to rudimentary marking of postulated morpheme boundaries in the word’s surface form. Because of the lack of morphotactical information, there is also no straightforward way to utilize such methods for generating new words: considering arbitrary morpheme sequences overgenerates massively and additional filtering approaches are needed, like the ones presented by (Rasooli et al., 2014). Finally, the notion of morpheme itself, although widely accepted in linguistics, has also been subject to criticism (e.g. Aronoff, 1976, 2007; Anderson, 1992).

An alternative linguistic theory, called Whole Word Morphology (Ford et al., 1997; Singh et al., 2003) (henceforth WWM), seems in our opinion particularly useful from the point of view of unsupervised learning. In WWM, the structural regularities between words are expressed as patterns operating simultaneously on multiple levels of lexical representation (phonological, syntactic, semantic). For example, the structural relationship between cat and cats would be captured by the following rule:\footnote{For the sake of simplicity, we discard the allophony in the phonological representation and present the semantic layer in an extremely schematic way.}

\[
\begin{bmatrix}
\text{PHON: } /X/ \\
\text{SYNT: } N, SG \\
\text{SEM: } \spadesuit
\end{bmatrix}
\leftrightarrow
\begin{bmatrix}
\text{PHON: } /Xs/ \\
\text{SYNT: } N, PL \\
\text{SEM: } \text{many } \spadesuit
\end{bmatrix}
\] (1)

The bidirectional arrow postulates, that if there is a word matching the pattern on one side of the rule, a counterpart matching the other side should also be a valid word. There is no notion of ‘internal word structure’ and neither of the words is
said to be morphologically ‘more complex’ than the other. The variable \(X\) stands for an arbitrary sequence of phonemes, which is retained on both sides of the rule. While the particular representations are further decomposable, for instance the phonological one in syllables and phonemes, the smallest unit of the language that combines all three layers is the word, and not the morpheme.

In this way, the morphological structure of a lexicon can be expressed as a graph, in which words constitute vertices and pairs of words following a regular structural pattern are connected with an edge, labeled with the corresponding rule. For the task of unsupervised learning, we see it as an advantage to learn a relation operating directly on observable objects (i.e. words), rather than some vaguely defined and theory-dependent underlying representation, like morpheme segmentation.

In the remainder of this paper, we briefly review previous unsupervised approaches to morphology (Sec. 2), present a generative probabilistic model for graphs of word derivations (Sec. 3), along with inference algorithms suited for unsupervised learning (Sec. 4). Our method is evaluated in Sec. 5.

2 Related Work

The approaches focusing on segmentation of words into smaller meaningful units have a long history, ranging from heuristic methods (Harris, 1955; Goldsmith, 2006) to the more recent approaches employing complete probabilistic models. A particularly successful example of the latter is Morfessor (Creutz and Lagus, 2005; Virpioja et al., 2013). Further probabilistic models include probabilistic hierarchical clustering (Can, 2011) and log-linear models (Poon et al., 2009). The yearly competition MorphoChallenge (Kurimo et al., 2010), which took place from 2005 until 2010, provides a good overview on the state of the art in morphological segmentation.

Another line of research concentrates on finding pairs of morphologically related words and using them to discover more general patterns. Various similarity measures are often used to identify such pairs, including orthographic and context similarity, or a combination of both (Yarowsky and Wicentowski, 2000; Baroni et al., 2002; Kirschenbaum, 2013). The first approach explicitly mentioning Whole Word Morphology as linguistic foundation has been presented by (Neuvel and Fulop, 2002), followed by a graph clustering method (Janicki, 2013) and a graph-based probabilistic model (Janicki, 2015). Recently, also word embeddings have been used to induce word-based transformation rules (Soricut and Och, 2015; Narasimhan et al., 2015). The latter method also produces graph-based representations of morphology, but is eventually evaluated on the segmentation task.

While, to our best knowledge, sampling from a probability distribution over graph structures has not yet been applied in the task of learning morphology, it has been successfully applied in other NLP tasks, notably unsupervised dependency parsing (Mareček, 2012; Teichmann, 2014) and machine translation (Peng and Gildea, 2014).

3 The Probabilistic Model

The model described here is a slight modification of the one introduced by (Janicki, 2015). Our goal is a probability distribution \(Pr(V, E|R)\) over graphs (consisting of a set of vertices \(V\) and a set of labeled edges \(E\)), given a set of transformation rules \(R\). A single graph represents a hypothesis about the origin of words: the root nodes constitute the idiosyncratic part of the lexicon, i.e. they correspond to words, that are not derived from any other and must be memorized. Once some words are introduced, further ones can be derived using the transformation rules. Such derivations correspond to edges leading to new nodes. We restrict the allowed structure of the graphs to directed forests: they must not contain cycles and every node has at most one ingoing edge, i.e. every word has a unique analysis. Accordingly, we consider directed transformation rules.

An example of such graph is shown in Fig. 1. In this case, relation is the base for the whole word family: it is used to derive, among others, related,
which in turn serves as a base for further words. Note that the tree shown in Fig. 1 does not constitute a linguistically correct analysis, nor does it have to. A unique ‘correct’ tree usually does not exist, e.g. the decision of whether the correct analysis of correlation should be correlate ← correlate or correlation ← relate, or yet another, is from our point of view completely arbitrary. This is the reason why we are not going to focus on single graphs, but rather on large samples, in which such multiple possibilities are accounted for.

Moving on to the probabilistic formulation of the model outlined above, let \( \rho \) be a probability distribution over strings, which should be nonzero at least for all well-formed words of the language. The root nodes of the graph are drawn from \( \rho \). Then, we iteratively try to apply every rule on every word, resulting in a (possibly empty) set of candidate derivations. Each derivation is an independent Bernoulli trial with probability \( \theta_r \): if it succeeds, the new word is introduced into the graph, along with the edge deriving it. We thus arrive at the following distribution:\(^3\)

\[
\Pr(V,E|R, \Theta_R) \propto \prod_{v \in V_0} \rho(v) \\
\times \prod_{v \in V} \prod_{r \in R} \prod_{r'(v') \in R(v)} \begin{cases} 
\theta_r & \text{if } \langle v, v', r \rangle \in E, \\
1 - \theta_r & \text{if } \langle v, v', r \rangle \notin E
\end{cases}
\]

\(V_0\) denotes the set of root nodes in the graph \((V,E)\). \(\Theta_R\) is the parameter vector, which contains \(\theta_r\) values for each rule \(r\). \(r(v)\) is the set of words derived from \(v\) by applying \(r\). Note that \(r(v)\) might be empty if \(v\) does not match the left-hand side of \(r\). As to the distribution \(\rho\), we learn it from the observed vocabulary \(V\) using the ALERGIA algorithm (de la Higuera, 2010), which learns distributions over strings from samples. Once learnt, it is considered fixed and not changed by our inference procedure.

Furthermore, let \(n_r\) denote the number of edges in the graph \((V,E)\) labeled with \(r\) and \(m_r\) denote the total number of words, that can be derived with \(r\) from words from \(V\). More formally:

\[
n_r := |\{(v, v', r') \in E : r' = r\}| \tag{3}
\]

\[
m_r := \sum_{v \in V} |r(v)| \tag{4}
\]

Then (2) can be rewritten as:

\[
Pr(V,E|R, \Theta_R) \propto \prod_{v \in V_0} \rho(v) \prod_{r \in R} \theta_r^{n_r}(1-\theta_r)^{m_r-n_r} \tag{5}
\]

From (5), we can easily see, that the number of edges derived by a rule follows a Binomial distribution. Following the Bayesian approach, we use Beta distribution as conjugate prior for \(\theta_r\):

\[
\theta_r \sim Be(\alpha, \beta) \tag{6}
\]

In practice, \(\alpha\) and \(\beta\) are always set to 1.1 (an almost uniform prior, but with exclusion of extreme values). The parameters can be integrated out:

\[
Pr(V,E|R) = \int_{(0,1)^{|R|}} Pr(V,E|R, \Theta_R) \times Pr(\Theta_R|R)d\Theta_R \propto \prod_{v \in V_0} \rho(v) \prod_{r \in R} B(n_r + \alpha, m_r - n_r + \beta) / B(\alpha, \beta) \tag{7}
\]

Finally, we introduce a probability distribution for the rule set. For this purpose, we represent the rules as sequences of edit operations. For example, the rule /X/ation/ → /X/ate/ deriving relate from relation is represented as the following sequence:

\[
* a:a t:t i:i e o:o n:n # \tag{8}
\]

The item denoted by * means leaving an arbitrary sequence of characters unchanged and # is a special item terminating the sequence. The probability \(\pi(r)\) of a rule is simply a product of the probabilities of individual sequence items (i.e. edit operations), which are treated as symbols of an alphabet. The item probabilities are learnt from the initial set of candidate rules and considered fixed, just like the \(\rho\) distribution for root words. The
probability of the rule set is then proportional to the product of probabilities of individual rules:

\[ Pr(R) \propto \prod_{r \in R} \pi(r) \quad (9) \]

The distribution \( Pr(R) \) penalizes complex models: it attributes lower probabilities to large rule sets and specific, sophisticated rules.

### 4 Inference

While (Janicki, 2015) used an optimization approach to find the single best graph, our goal is to base the inference on large samples from the distribution over graphs using a Markov Chain Monte Carlo sampler. In particular, we are going to be interested in expected values of certain functions of the graph with respect to the edge structure, which is a latent variable. Thus, for a given function \( h \) (e.g. measuring the frequency of a rule or the likelihood of the graph), we want to be able to approximate the expectations of the following form:

\[ \mathbb{E}_{E \mid V, R} h(V, E) = \sum_{E} h(V, E) Pr(E \mid V, R) \quad (10) \]

#### 4.1 Finding Candidate Rules

We begin by extracting all pairs of words that might be morphologically related from the given vocabulary. We follow the approach of (Janicki, 2015): we apply a modified FastSS algorithm (Bocek et al., 2007) to find all pairs of words, that differ with at most 5 characters at the beginning and at the end and with at most 3 characters within a single slot inside the word. Those numbers are configurable parameters, but we have found the above values to be sufficient to capture most morphological rules in many languages.

Each pair of words is used to extract a number of transformation rules of the form (cf. (1)):

\[ /a_1X_1a_2X_2a_3/ \rightarrow /b_1X_1b_2X_2b_3/ \quad (11) \]

where \( X_1, X_2 \) are variable elements, \( a_1, a_3, b_1, b_3 \) are constants of at most 5 characters, and \( a_2, b_2 \) are constants of at most 3 characters.\(^4\) There are usually many rules that can be derived from a single pair of words, depending on whether we assign the common substrings of both words to the variable elements \( X_1, X_2 \), resulting in more general rules, or to the constants, resulting in more specific rules.

4In case \( a_2 \) and \( b_2 \) are both empty, \( X_1 \) and \( X_2 \) are merged into a single variable \( X \).

For example, three of many rules that can be extracted from the pair \( \langle \text{relate}, \text{correlate} \rangle \) are given below:

\[ /X/ \rightarrow /\text{cor}X/ \]
\[ /rX/ \rightarrow /\text{corr}X/ \]
\[ /rX\text{ate}/ \rightarrow /\text{corr}X\text{ate}/ \quad (12) \]

In order to reduce the number of candidate rules and edges to tractable sizes, we apply the following filtering criteria:

- **max. number of rules**: only \( N_{\text{max}} \) most frequent rules are kept;
- **max. number of edges per word pair**: only \( k \) most general rules are extracted from each word pair;
- **min. rule frequency**: only rules occurring in at least \( n_{\text{min}} \) word pairs are kept.

In all our experiments, we used fixed values of \( N_{\text{max}} = 10000, k = 5, n_{\text{min}} = 3 \), which led to good results for training data of various sizes. Those values can thus be safely used as default setting, without the need of parameter tuning.

#### 4.2 The Sampler

Having a set of rules \( R \) and a vocabulary \( V \), we are ready to draw samples of edge sets from the distribution \( Pr(E \mid V, R) \), which is proportional to \( Pr(V, E \mid R) \) up to a normalizing constant. In the following, we will define a sampler based on the Metropolis-Hastings algorithm, which belongs to a larger family of Markov Chain Monte Carlo methods.

The key idea of Markov Chain Monte Carlo methods is, given a probability distribution \( f \), to construct a Markov chain, for which \( f \) is the limiting distribution (Robert and Casella, 2005). The Metropolis-Hastings algorithm (Metropolis et al., 1953; Hastings, 1970) provides a relatively simple recipe for such chain. It involves an instrumental distribution \( q(y \mid x) \) used to propose the next item \( y \) of the sample given the current item \( x \). Then, the next item of the sample is taken to be either \( y \) or \( x \), depending on whether the proposal is accepted or rejected. The probability of acceptance is:

\[ \alpha(x, y) = \min \left\{ \frac{f(y) q(x \mid y)}{f(x) q(y \mid x)}, 1 \right\} \quad (13) \]

Note that the distributions \( f \) and \( q \) only have to be known up to a multiplicative constant, since the
computation only involves quotients of their values. Also, \( q \) does not have to bear any relationship to \( f \). It is sufficient that every point of the sample space, for which \( f \) is nonzero, can be reached from any other in a finite number of steps using \( q \). Then (13) implies that the resulting Markov chain has \( f \) as its limiting distribution. Although the sample obtained from such chain is not independent, it can be used for approximating expectations like (10).

The preprocessing step described in the previous section provides us with a set of all candidate edges \( \mathcal{E} \), which can be created by the rules from \( R \). The idea for a proposal distribution \( q(\cdot|E) \), given the current set of edges \( E \), is the following: we choose an edge \( e \) uniformly from \( \mathcal{E} \). If it is already present in \( E \), we delete it, if not, we add it. In this way, we obtain a proposal for the next set of edges \( E' \). Note that in this way we can reach any graph from any other in a finite number of steps by first deleting all the edges of the first graph and then adding all the edges of the second graph one by one.

There is however one problem with this approach: while deleting an edge is always possible, adding one could result in an ill-formed graph (e.g. create a cycle). If we simply discarded such proposals and proposed staying with the current graph instead, such procedure would still yield a valid instrumental distribution and a valid MCMC sampler. While the resulting chain would still be theoretically correct, its so-called mixing properties would be very bad, meaning that it would need an extremely large number of iterations to converge to the limiting distribution. For this reason, we are going to introduce additional moves which make adding of an edge possible in most cases.

Let’s consider adding a new edge \( v_1 \to v_2 \). The first problematic case is when the new edge would create a cycle, i.e. \( v_1 \) is already a descendant of \( v_2 \). Let \( v_3 \) denote the parent of \( v_2 \), \( v_5 \) the immediate child of \( v_2 \) which leads to \( v_1 \) and \( v_4 \) the parent of \( v_1 \) (see Fig. 2). We have two possibilities to add an edge between \( v_1 \) and \( v_2 \) by ‘cutting out’ either \( v_1 \) or \( v_2 \) from its place in the tree. Both variants involve adding and deleting two edges. We refer to this kind of operation as ‘flip’. The variant to be used is chosen randomly each time a ‘flip’ move is to be applied. Note that a ‘flip’ move might be impossible if the other edge to be added (\( v_3 \to v_1 \) or \( v_3 \to v_5 \), respectively) is not available in \( \mathcal{E} \).

In this case, we propose staying with the current graph, which, as already mentioned, does not undermine the validity of the sampler. The absence of other involved edges (e.g. \( v_3 \to v_2 \) in case \( v_2 \) is a root) or the overlapping of some nodes (e.g. \( v_5 = v_1 \) and \( v_4 = v_2 \) if \( v_1 \) is a child of \( v_2 \) directly) can be simply ignored as the move is still valid.

Another problematic case arises when the newly added edge \( v_1 \to v_2 \) would not create a cycle, but \( v_2 \) already has an ingoing edge (possibly even from \( v_1 \), but with a different label). In this case, we simply exchange the previous ingoing edge of \( v_2 \) for the new one.

It is important to point out, that all moves are reversible and that the resulting proposal distribution is symmetric. The move is uniquely determined by the choice of the edge \( e \) to be added or deleted, except for the ‘flip’ case, where additionally one of the two variants of the move is randomly chosen. In case of adding or removing a single edge without side effects, selecting the same edge again reverses the operation. If the edge to be added is exchanged for another, selecting the previously deleted edge will reverse it. Finally, the first variant of ‘flip’ on \( v_1 \to v_2 \) can be reversed by the second variant on \( v_4 \to v_1 \) and the second variant on \( v_1 \to v_2 \) can be reversed by the first variant on \( v_2 \to v_5 \).

Note, that the complexity of a single sampling iteration is only \( O(h) \), with \( h \) being the maximum height of a tree, since \( h \) operations are needed to determine whether \( v_1 \) is a descendant of \( v_2 \). In practice, \( h \) is usually bounded by a small constant. Also, we do not need to memorize the graphs seen in the sample, we only have to keep track of the current graph and the current values of the expectations we are interested in. The latter can be up-

Figure 2: The two variants of the ‘flip’ operation. The deleted edges are dashed and the newly added edges dotted. The goal of the operation is to make possible adding an edge from \( v_1 \) to \( v_2 \) without creating a cycle.
dated dynamically. A single sampling iteration is thus computationally very cheap, which enables us to draw large samples. In the experiments, we use sample sizes of 50 million graphs.

4.3 Model Selection

The sampler developed in the previous section has multiple applications. One of them is model selection, i.e. the task of selecting an optimal set of rules. For the purpose of comparing models, we introduce the following expected log-likelihood function:

\[
\ell(R) = \mathbb{E}_{V,R} \ln \Pr(V, E|R) + \ln \Pr(R)
\]

\[
= \mathbb{E}_{V,R} \left[ \sum_{v \in V_0} \ln \rho(v) \right]
+ \sum_{r \in R} \ln B(n_r + \alpha, m_r - n_r + \beta)
- |R| \ln B(\alpha, \beta) + \sum_{r \in R} \ln \pi(r) \quad (14)
\]

We use the graph sampler for computing the value of \( \ell(R) \) for a single rule set. The model selection task is to maximize \( \ell \), i.e. to find:

\[
\hat{R} = \arg \max_R \ell(R) \quad (15)
\]

For this optimization task, we use the simulated annealing algorithm (Kirkpatrick et al., 1983), which is closely related to MCMC sampling. In this algorithm, we also use an instrumental distribution \( q(y|x) \) to propose the next point \( y \) given the current point \( x \). Let \( h \) denote the function to optimize. Then the acceptance probability of \( y \) while being at \( x \) is defined as:

\[
\alpha(x, y) = \min \left\{ \frac{q(x|y)}{q(y|x)} e^{h(y)-h(x)}, 1 \right\} \quad (16)
\]

The parameter \( t \) is called temperature and is meant to decrease with each iteration, thus decreasing the algorithm’s willingness to move to points with lower \( h \) value. As (Besag, 2004) points out, if we consider a distribution \( f(x) \propto \exp h(x) \), then simulated annealing corresponds to MCMC sampling from a distribution proportional to \( f^{1/t} \). As \( t \) goes towards zero, the latter will converge to a uniform distribution over global maxima of \( h \). In this way, the algorithm is able to find a global maximum and escape local maxima.

We are now going to define the instrumental distribution \( q(R'|R) \) used to propose the next rule set. All considered rule sets are going to be subsets of \( R \), which denotes the set of rules obtained after the preprocessing step described in Sec. 4.1. We begin by defining the score of a single rule, which is the expected contribution of this rule to the log-likelihood of the graph:

\[
\zeta(r) = \mathbb{E}_{E|V,R} \left[ - \sum_{(v, v', r') \in E} \ln \rho(v') 
+ \ln B(n_r + \alpha, m_r - n_r + \beta) 
- \ln B(\alpha, \beta) + \ln \pi(r) \right] \quad (17)
\]

The first term corresponds to the log-likelihood, that is gained by deriving words using \( r \), rather than having them as roots. We subsequently apply the logistic function to turn the rule score into a probability:

\[
g(r) = \frac{1}{1 + \exp(-\gamma \cdot \zeta(r))} \quad (18)
\]

where \( \gamma \) is a configurable parameter. \( g(r) \) is the probability of \( r \) being selected to the next rule set. Note that \( g(r) \) is also defined for rules not occurring in the current rule set: the first term and \( n_r \) are then simply always zero. Finally, we propose the next rule set \( R' \) by randomly determining for each rule from \( R \), whether it is going to be selected or not. Basing the selection probability on \( \zeta(r) \) means that the chances of a rule to ‘survive’ in the next iteration depend on its usefulness in the current iteration. Once a rule is dropped, it can still be re-selected, but the probability of it happening is rather small. Finally, \( \gamma \) is set to be equal to inverse temperature of the annealing algorithm, which means that the importance of rule performance increases over time, allowing less and less changes in later iterations.

In practice, the cost of one iteration of the annealing algorithm is high, since it involves a whole run of the graph sampler. We are thus only going to perform a few annealing iterations (typically 20 or 30) which is obviously not enough to find the global maximum. Thus, we use this algorithm only as a local optimizer: to reduce the set of rules as much as possible within a reasonable runtime. However, it is still a plausible choice because of its flexibility, e.g. being able to move across a parameter space composed of discrete sets (unlike e.g.
the EM algorithm, which requires a space of real-valued vectors).

4.4 Model Fitting

Once the optimal model is selected, we can determine optimal values for the parameter vector \( \Theta_R \). For this purpose, we use the Monte Carlo EM algorithm (Wei and Tanner, 1990), which is a variant of EM using a sampler to approximate the expected values. In the maximization step, we set the \( \theta_r \) values to their maximum a-posteriori likelihood estimates:

\[
\theta_r^{(t+1)} := \frac{E_{E[V,R,W]}[n_r] + \alpha - 1}{m_r + \alpha + \beta - 2}
\] (19)

5 Evaluation

We evaluate our approach on the tasks of morphological analysis and generation.

5.1 Analysis

As we intend to avoid postulating internal word structure, the task of analysis is defined as linking an unknown word to morphologically similar words from a known lexicon. We consider a pair of words to be morphologically similar if one word can be derived from the other using a single morphological operation (e.g. affix insertion, deletion or substitution). Pairs of morphologically similar words can also be extracted from segmentations by computing edit distance on morpheme sequences – words are considered morphologically similar if such distance is equal to 1 and the difference does not include stems.

Dataset We use the CELEX lexical database to derive training and evaluation data. CELEX provides data for English, German and Dutch, including morphological segmentation, labeling of inflectional classes and corpus frequency. For training, we use words with nonzero corpus frequency, while the remaining words, i.e. those with zero frequency, constitute the testing dataset. The size of the datasets is shown in Table 1.

<table>
<thead>
<tr>
<th></th>
<th>training</th>
<th>testing</th>
</tr>
</thead>
<tbody>
<tr>
<td>English</td>
<td>45,391</td>
<td>15,608</td>
</tr>
<tr>
<td>German</td>
<td>76,813</td>
<td>221,190</td>
</tr>
<tr>
<td>Dutch</td>
<td>103,190</td>
<td>145,354</td>
</tr>
</tbody>
</table>

Table 1: The size (number of words) of datasets used for the analysis task.

<table>
<thead>
<tr>
<th>Language</th>
<th>Model</th>
<th>Precision</th>
<th>Recall</th>
<th>F-score</th>
</tr>
</thead>
<tbody>
<tr>
<td>English</td>
<td>Morfessor –MS</td>
<td>74.4 %</td>
<td>41.4 %</td>
<td>53.2 %</td>
</tr>
<tr>
<td></td>
<td>+MS</td>
<td>38.5 %</td>
<td>73.2 %</td>
<td>50.5 %</td>
</tr>
<tr>
<td>German</td>
<td>Morfessor –MS</td>
<td>75.1 %</td>
<td>37.8 %</td>
<td>51.2 %</td>
</tr>
<tr>
<td></td>
<td>+MS</td>
<td>56.4 %</td>
<td>67.8 %</td>
<td>61.6 %</td>
</tr>
<tr>
<td>Dutch</td>
<td>Morfessor –MS</td>
<td>73.1 %</td>
<td>39.2 %</td>
<td>51.0 %</td>
</tr>
<tr>
<td></td>
<td>+MS</td>
<td>42.5 %</td>
<td>68.1 %</td>
<td>52.3 %</td>
</tr>
</tbody>
</table>

Table 2: The model size (number of rules) before and after model selection.

<table>
<thead>
<tr>
<th>Language</th>
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<td>+MS</td>
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<td>52.3 %</td>
</tr>
</tbody>
</table>

Table 3: Results for the analysis task.

Experiment setup We report the results for two different setups: with model selection (+MS) and without it (–MS). We also compare our results to Morfessor Categories-MAP (Creutz and Lagus, 2005). In addition to morpheme segmentations, this tool labels each morpheme as prefix, affix or stem, which enables us to convert its output into morphologically similar pairs using the edit distance method. The training dataset also constitutes the known lexicon, i.e. we evaluate pairs of similar words \((w_1, w_2)\) with \(w_1\) coming from the training and \(w_2\) from the testing dataset.

Results The results are shown in Table 3. The setup with model selection achieves the best performance for all three languages, which demonstrates the usefulness of this step. The difference is especially clear for English, where the setup without model selection performs worse than Morfessor. Our method also manages to capture non-concatenative morphology: pairs like German \((\text{findet}, \text{f"andet})\) or Dutch \((\text{televisiekanaal}, \text{televisiekanaal})\), are successfully detected. On the other hand, the method based on Morfessor segmentations suffers from low recall: even small errors in segmentation can result in a failure to discover many similar pairs.

Table 2 shows another benefit of model selection: reducing the number of rules approximately by half, which has a significant impact on the speed of the analysis.

Unfortunately, such conversion is not possible for most other approaches to unsupervised segmentation, which do not provide additional labeling for stems.
<table>
<thead>
<tr>
<th>Language</th>
<th>Model</th>
<th>1k</th>
<th>5k</th>
<th>10k</th>
<th>50k</th>
<th>100k</th>
<th>200k</th>
<th>500k</th>
</tr>
</thead>
<tbody>
<tr>
<td>English</td>
<td>–MS, –F</td>
<td>72.2%</td>
<td>52.5%</td>
<td>48.4%</td>
<td>37.3%</td>
<td>26.9%</td>
<td>20.4%</td>
<td>11.1%</td>
</tr>
<tr>
<td></td>
<td>–MS, +F</td>
<td>69.8%</td>
<td>64.9%</td>
<td>62.3%</td>
<td>42.5%</td>
<td>31.1%</td>
<td>22.3%</td>
<td>17.5%</td>
</tr>
<tr>
<td></td>
<td>+MS, +F</td>
<td>71.9%</td>
<td>66.4%</td>
<td>62.7%</td>
<td>43.4%</td>
<td>32.7%</td>
<td>22.9%</td>
<td>17.0%</td>
</tr>
<tr>
<td>German</td>
<td>–MS, –F</td>
<td>85.6%</td>
<td>80.0%</td>
<td>74.3%</td>
<td>56.0%</td>
<td>42.3%</td>
<td>32.2%</td>
<td>17.5%</td>
</tr>
<tr>
<td></td>
<td>–MS, +F</td>
<td>86.0%</td>
<td>82.0%</td>
<td>83.7%</td>
<td>68.0%</td>
<td>51.2%</td>
<td>35.7%</td>
<td>21.4%</td>
</tr>
<tr>
<td></td>
<td>+MS, +F</td>
<td>86.4%</td>
<td>83.0%</td>
<td>83.9%</td>
<td>67.8%</td>
<td>51.5%</td>
<td>35.9%</td>
<td>21.1%</td>
</tr>
<tr>
<td>Dutch</td>
<td>–MS, –F</td>
<td>50.0%</td>
<td>53.3%</td>
<td>53.3%</td>
<td>31.6%</td>
<td>24.6%</td>
<td>18.0%</td>
<td>10.3%</td>
</tr>
<tr>
<td></td>
<td>–MS, +F</td>
<td>73.9%</td>
<td>60.1%</td>
<td>60.5%</td>
<td>38.7%</td>
<td>29.4%</td>
<td>20.6%</td>
<td>11.2%</td>
</tr>
<tr>
<td></td>
<td>+MS, +F</td>
<td>73.9%</td>
<td>62.2%</td>
<td>62.2%</td>
<td>38.8%</td>
<td>29.8%</td>
<td>21.0%</td>
<td>11.4%</td>
</tr>
</tbody>
</table>

Table 4: Results for the generation task. The scores show precision depending on the number of generated words. (‘k’ means ‘thousand’).

5.2 Generation

In generation task, we evaluate the capability of the model to derive new, valid words using the learnt morphological rules. As the recall measure for this task is hardly possible to compute (it would involve listing all and only words derivable from the training set), we evaluate the precision against the number of generated words.

Dataset  For training, we use the same datasets as in the analysis task (CELEX words with nonzero corpus frequency). The testing wordlists, which are supposed to contain at least all words obtainable from the training words within a single morphological operation, are built by merging the complete CELEX vocabulary with lists of Wiktionary entries for the relevant language.

Experiment setup  We conduct the experiment on three different settings, depending on whether the model selection (MS) and the fitting (F) step are carried out or omitted. In case of omitting the fitting step, the rule probabilities ($\theta_r$) are set according to (19), but using maximum rule frequency, i.e. the number of candidate edges in $\mathcal{E}$ labeled with this rule, as $n_r$. The generated words are ordered by their contribution to the log-likelihood of the data, which is equivalent to sorting according to the probability of the rule used to derived the word.

For this task, we do not include any comparison to a segmentation-based approach. Such approaches usually do not model morphotactics at all, or do it in a very simple way (like Morfessor Categories-MAP). Applying them to generate new words leads to a disastrous overgeneration (e.g. every common morpheme can be repeated many times), which renders a comparison pointless. Segmentation models are simply not designed for the generation task.

Results  The results shown in Table 4 highlight the importance of a proper fitting step, which in most cases improves the results considerably. On the other hand, the impact of the model selection step is rather insignificant. This is understandable: the goal of model selection is to eliminate weak, useless rules, while in the word generation task, the strongest rules are applied first.

6 Conclusion

We have presented a method for unsupervised discovery of pairs of morphologically related words without performing morpheme segmentation. Our method is based on a probabilistic model describing graphs of word derivations. We developed a Markov Chain Monte Carlo sampler for such graphs, which allows us to approximate expectations over the latent edge structure. The evaluation results confirm our intuition, that the discovery of morphologically related words, as well as prediction of unseen words, is easier without the need of morpheme segmentation. While we limited ourselves to unannotated string forms of words, the formalism can be easily extended to include various other word features, like POS-tags or frequency. In the further work, we especially intend to follow the recent trend and include word embeddings as a feature. Furthermore, we are going to examine practical applications of a whole-word morphology model, like e.g. increasing the performance of statistical language models in dealing with unknown words. We believe that morpheme segmentation is neither sufficient nor necessary for learning morphology, especially in the unsupervised setting.

7The results for the +MS, –F case are omitted, because they are very similar to –MS, –F, and thus do not contribute anything noteworthy to the evaluation.
References


Mark Aronoff. 2007. In the Beginning was the Word. Language 83(4):803–830.


